| $\operatorname{Pr}(F \leq 1)$ | $r_{3}$ | 1 | 2 | 3 | 4 | 5 | $6^{\prime}$ | 7 | 8 | 9 | 10 | 12 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.95 | 6 | 5.99 | 5.14 | 4.76 | 4.53 | 4.39 | 4.28 | 4.21 | 4.15 | 4.10 | 4.06 | 4.00 | 3.94 |
| 0.975 |  | 8.81 | 7.26 | 6.60 | 6.23 | 5.99 | 5.82 | 5.70 | 5.60 | 5.52 | 5.46 | 5.37 | 5.27 |
| 0.99 |  | 13.7 | 10.9 | 9.78 | 9.15 | 8.75 | 8.47 | 8.26 | 8.10 | 7.98 | 7.87 | 7.72 | 7.56 |
| 0.95 | 7 | 5.59 | 4.74 | 4.35 | 4.12 | 3.97 | 3.87 | 3.79 | 3.73 | 3.68 | 3.64 | 3.57 | 3.51 |
| -0.975 |  | 8.07 | 6.54 | 5.89 | 5.52 | 5.29 | 5.12 | 4.99 | 4.90 | 4.82 | 4.76 | 4.67 | 4.57 |
| 0.99 |  | 12.2 | 9.55 | 8.45 | 7.85 | 7.46 | 7.19 | 6.99 | 6.84 | 6.72 | 6.62 | 6.47 | 6.31 |
| 0.95 | 8 | 5.32 | 4.46 | 4.07 | 3.94 | 3.69 | 3.58 | 3.50 | 3.44 | 3.39 | 3.35 | 3.28 | 3.22 |
| 0.975 |  | 7.57 | 6.06 | 5.42 | 5.05 | 4.82 | 4.65 | 4.53 | 4.43 | 4.36 | 4.30 | 4.20 | 4.10 |
| 0.99 |  | 11.3 | 8.65 | 7.59 | 7.01 | 6.63 | 6.37 | 6.18 | 6.03 | 5.91 | 5.81 | 5.67 | 5.52 |
| 0.95 | 9 | 5.12 | 4.26 | 3.36 | 3.63 | 3.48 | 3.37 | 3.29 | 3.23 | 3.18 | 3.14 | 3.07 | 3.01 |
| 0.975 |  | 7.21 | 5.71 | 5.08 | 4.72 | 4.48 | 4.32 | 4.20 | 4.10 | 4.03 | 3.96 | 3.87 | 3.77 |
| 0.99 |  | 10.6 | 8.02 | 6.99 | 6.42 | 6.06 | 5.80 | 5.61 | 5.47 | 5.35 | 5.26 | 5.11 | 4.96 |
| 0.95 | 10 | 4.96 | 4.10 | 3.71 | 3.48 | 3.33 | 3.22 | 3.14 | 3.07 | 3.02 | 2.98 | 2.91 | 2.85 |
| 0.975 |  | 6.94 | 5.46 | 4.83 | 4.47 | 4.24 | 4.07 | 3.95 | 3.85 | 3.78 | 3.72 | 3.62 | 3.52 |
| 0.99 |  | 10.0 | 7.56 | 6.55 | 5.99 | 5.64 | 5.39 | 5.20 | 5.06 | 4.94 | 4.85 | 4.71 | 4.56 |
| 0.95 | 12 | 4.75 | 3.89 | 3.49 | 3.26 | 3.11 | 3.00 | 2.91 | 2.85 | 2.80 | 2.75 | 2.69 | 2.62 |
| 0.975 |  | 6.55 | 5.10 | 4.47 | 4.12 | 3.89 | 3.73 | 3.61 | 3.51 | 3.44 | 3.37 | 3.28 | 3.18 |
| 0.99 |  | 9.33 | 6.93 | 5.95 | 5.41 | 5.06 | 4.82 | 4.64 | 4.50 | 4.39 | 4.30 | 4.16 | 4.01 |
| 0.95 | 15 | 4.54 | 3.68 | 3.29 | 3.06 | 2.90 | 2.79 | 2.71 | 2.64 | 2.59 | 2.54 | 2.48 | 2.40 |
| 0.975 |  | 6.20 | 4.77 | 4.15 | 3.80 | 3.58 | 3.41 | 3.29 | 3.20 | 3.12 | 3.06 | 2.96 | 2.86 |
| 0.99 |  | 8.68 | 6.36 | 5.42 | 4.89 | 4.56 | 4.32 | 4.14 | 4.00 | 3.89 | 3.80 | 3.67 | 3.52 |

- This tabie is abridged and adapted from " Tables of Percentage Points of the Inverted Beta Distribution," Biometrika, 33 (1943). It is published here with the kind permission of Professor E. S. Pearson on behalf of the authors, Maxine Merrington and Catherine M. Thampson. and of the Biometrika Trustees.

TABLE II
The Chi-Square Distribution*
$\operatorname{Pr}(X \leq x)=\int_{0}^{x} \frac{1}{\Gamma(r / 2) 2^{r / 2}} w^{r / 2-1} c^{-w / 2} d w$

| $r$ | $\operatorname{Pr}(X \leq x)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0.01 | 0.025 | 0.050 | 0.95 | 0.975 | 0.99 |
| 1 | 0.000 | 0.001 | 0.004 | 3.84 | 5.02 | 6.63 |
| 2 | 0.020 | 0.051 | 0.103 | 5.99 | 7.38 | 9.21 |
| 3 | 0.115 | 0.216 | 0.352 | 7.81 | 9.35 | 11.3 |
| 4 | 0.297 | 0.484 | 0.711 | 9.49 | 11.1 | 13.3 |
| 5 | 0.554 | 0.831 | 1.15 | 11.1 | 12.8 | 15.1 |
| 6 | 0.872 | 1.24 | 1.64 | 12.6 | 14.4 | 16.8 |
| 7 | 1.24 | 1.69 | 2.17 | 14.1 | 16.0 | 18.5 |
| 8 | 1.65 | 2.18 | 2.73 | 15.5 | 17.5 | 20.1 |
| 9 | 2.09 | 2.70 | 3.33 | 16.9 | 19.0 | 21.7 |
| 10 | 2.56 | 3.25 | 3.94 | 18.3 | 20.5 | 23.2 |
| 11 | 3.05 | 3.82 | 4.57 | 19.7 | 21.9 | 24.7 |
| 12 | 3.57 | 4.40 | 5.23 | 21.0 | 23.3 | 26.2 |
| 13 | 4.11 | 5.01 | 5.89 | 22.4 | 24.7 | 27.7 |
| 14 | 4.66 | 5.63 | 6.57 | 23.7 | 26.1 | 29.1 |
| 15 | 5.23 | 6.26 | 7.26 | 25.0 | 27.5 | 30.6 |
| 16 | 5.81 | 6.91 | 7.96 | 26.3 | 28.8 | 32.0 |
| 17 | 6.41 | 7.56 | 8.67 | 27.6 | 30.2 | 33.4 |
| 18 | 7.01 | 8.23 | 9.39 | 28.9 | 31.5 | 34.8 |
| 19 | 7.63 | 8.91 | 10.1 | 30.1 | 32.9 | 36.2 |
| 20 | 8.26 | 9.59 | 10.9 | 31.4 | 34.2 | 37.6 |
| 21 | 8.90 | 10.3 | 11.6 | 32.7 | 35.5 | 38.9 |
| 22 | 9.54 | 11.0 | 12.3 | 33.9 | 36.8 | 40.3 |
| 23 | 10.2 | 11.7 | 13.1 | 35.2 | 38.1 | 41.6 |
| 24 | 10.9 | 12.4 | 13.8 | 36.4 | 39.4 | 43.0 |
| 25 | 11.5 | 13.1 | 14.6 | 37.7 | 40.6 | 44.3 |
| 26 | 12.2 | 13.8 | 15.4 | 38.9 | 41.9 | 45.6 |
| 27 | 12.9 | 14.6 | 16.2 | 40.1 | 43.2 | 47.0 |
| 28 | 13.6 | 15.3 | 16.9 | 41.3 | 44.5 | 48.3 |
| $29$ | $14.3$ | 16.0 | 17.7 | 42.6 | 45.7 | 49.6 |
| 30 | 15.0 | 16.8 | 18.5 | 43.8 | 47.0 | 50.9 |

- This table is abridged and adapted from "Tables of Percentage Pointa of the lucumplete Beta Function and of the Chi-Square Distribution," Biometrika, 32 (1941). It is pubtished here with the kind permission of Professor E. S. Pearson on behalf of whe author, Catherine M. Thumpson, and of the Biometrika Trustees.


## The t Distrlbution



$$
|\operatorname{Pr}(T \leq-1)=1-\operatorname{Pr}(T \leq 1)|
$$

| 1 | $\operatorname{Pr}(T \leq t)$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0.90 | 0.95 | 0.975 | 0.99 | 0.995 |
| 1 | 3078 | 6.314 | 12.106 | 31.821 | 63.657 |
| 2 | 1886 | 2.920 | 4.303 | 6.965 | 9.925 |
| 3 | 1.638 | 2.353 | 3.182 | 4.541 | 5.841 |
| 4 | 1.533 | 2.132 | 2.776 | 3.741 | 4.604 |
| 5 | 1.476 | 2015 | 2.571 | 3.365 | 4032 |
| 6 | 1.440 | 1.943 | 2.447 | 3.143 | 3.701 |
| 7 | 1.415 | 1.895 | 2.365 | 2.998 | 3.499 |
| 8 | 1.391 | 1860 | 2.306 | 2.896 | 3.355 |
| 9 | 1.383 | 1.833 | 2.262 | 2.821 | 3.250 |
| 10 | 1.372 | 1.812 | 2.228 | 2.764 | 3.169 |
| 11 | 1363 | 1.796 | 2.201 | 2.718 | 3.106 |
| 12 | ，1．356 | 1.782 | 2.179 | 2.681 | 3.055 |
| 13 | 1.350 | 1.771 | 2.160 | 2.650 | 3.012 |
| 14 | 1.345 | 1.761 | 2.145 | 2.624 | 2.977 |
| Is | 1.341 | 1.753 | 2.131 | 2.602 | 2.947 |
| 16 | 1.337 | 1.746 | 2.120 | 2.583 | 2.921 |
| 17 | 1.333 | 1.740 | 2.110 | 2.567 | 2.898 |
| 18 | 1.330 | 1.734 | 2.101 | 2.552 | 2.878 |
| 19 | 1328 | 1.729 | 2.093 | 2.539 | 2.861 |
| 29 | 1.325 | 1.725 | 2.086 | 2.528 | 2.845 |
| 21 | 1.323 | 1.721 | 2.080 | 2.518 | 2.831 |
| 22 | 1.321 | 1.717 | 2.074 | 2.508 | 2.819 |
| 23 | 1.319 | 1.714 | 2.069 | 2.500 | 2.807 |
| 24 | 1.318 | 1.711 | 2.061 | 2.492 | 2.797 |
| 25 | 1.316 | 1.708 | 2.060 | 2.485 | 2.787 |
| 26 | 1.315 | 1.706 | 2.056 | 2.479 | 2.779 |
| 21 | 1.314 | 1.703 | 2.052 | 2.473 | 2.771 |
| 28 | 1.313 | 1.701 | 2.048 | 2.467 | 2.763 |
| 29 | 1311 | 1.699 | 2.045 | 2.462 | 2.756 |
| 30 | 1.310 | 1.697 | 2.042 | 2.457 | 2.750 |

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| $n$ |  |  | SMo | $\begin{aligned} & \circ \circ \text { or } \\ & \cdots \\ & \infty \\ & \infty \\ & \infty \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\sim$ | 管尤 $\frac{0}{6}$ | vivo | （i）${ }_{\text {y }}$ | $$ |  |
| $\bigcirc$ | $\begin{gathered} \text { No } \\ \text { co } \\ \sim \\ \sim \end{gathered}$ |  |  | $\begin{array}{lll} 0 & \mathrm{y} & \text { n } \\ \therefore & \text { os } \\ & \text { on } \\ \hline \end{array}$ |  |
| o， | 牙俞 |  |  | $\begin{array}{lll} 8 & 8 \\ 0 & 1 \\ 0 & 1 \end{array}$ |  |
| $\infty$ |  |  |  |  | $\begin{array}{ccc} \alpha & \cdots \\ \hdashline & \cdots & \cdots \\ \hdashline & 0 & 0 \end{array}$ |
| N | $\stackrel{\sim}{\sim} \stackrel{\infty}{\mathrm{y}} \stackrel{\infty}{\circ}$ | $\begin{array}{cc} \mathrm{o} \\ \text { ov } \\ \text { o } \\ \text { o } \end{array}$ | a $\infty$ $\infty$ $\infty$ $\sim$ |  | $\begin{array}{ccc} \infty & \text { n } \\ \infty & n \\ \text { v } & 0 & 0 \\ \hline \end{array}$ |
| $\because$ |  |  |  |  |  |
| $\checkmark$ |  | $\begin{array}{ll} m & m \\ o \\ o \\ o & 0 \\ o \end{array}$ |  |  |  |
| $\sim$ | $\underset{\sim}{\sim} \underset{\sim}{\sim}$ | $\propto$ | $\bar{o} \underset{\sim}{o v} \underset{\sim}{\sim} \underset{\sim}{\infty}$ | $\begin{aligned} & \text { y } \\ & \text { min n } \\ & \text { in } \end{aligned}$ | no |
| ч | స్ | $\begin{aligned} & \text { y } \underset{\sim}{1} \underset{\sim}{o} \\ & \text { or } \end{aligned}$ | $\frac{\pi}{o v} \underset{\sim}{c}$ |  | ov 品 |
| m | $\begin{array}{ccc} \cdots & \text { y } \\ \cdots & \underset{y}{c} & \\ \hline \end{array}$ |  | $\stackrel{\text { a }}{\sim}$ |  | $\begin{gathered} \bar{v} \\ \underset{\sim}{c} \underset{\sim}{c} \end{gathered}$ |
| $\sim$ | $\underset{\sim}{8} \underset{\sim}{8} \underset{\sim}{\circ} \underset{9}{\circ}$ |  | $\begin{array}{ll} n \\ n & 0 \\ 0 & 0 \\ 0 \end{array}$ |  |  |
| － |  |  | $\overline{\mathrm{o}}$ ¢ | rer | ¢om |
| $\because$ | r | N | $m$ | $v$ | in |
| $\begin{aligned} & \text { e } \\ & \mathrm{VI} \\ & \stackrel{U}{2} \end{aligned}$ | $$ | $\begin{array}{lll} \sim & \pi & o \\ \alpha & o & 0 \\ 0 & 0 & 0 \\ 0 & 0 \end{array}$ | $\begin{array}{ll} n & n \\ \vdots & 0 \\ o & 0 \\ 0 & 0 \\ 0 & 0 \end{array}$ |  | $$ |


[^0]:    －Ihas Lable ivabingeal from Iable 111 of Visher and Vates：Statistical Tables for
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